

STUDY TIPS

AS1.2: ALGEBRAIC SUBSTITUTION

The process of replacing a *pronumeral* (or variable or letter) in an expression or formula with a number is called *substitution*.

It is then possible to *evaluate* the algebraic expression.

Examples

1. Evaluate $3p$ if $p = -5$

$$\begin{aligned}3p &= 3 \times p \\ &= 3 \times -5 \\ &= -15\end{aligned}$$

2. Evaluate $\frac{a+5}{b}$ if $a = -9$ and $b = 2$

$$\begin{aligned}\frac{a+5}{b} &= \frac{-9+5}{2} \\ &= \frac{-4}{2} \\ &= -2\end{aligned}$$

3. Evaluate $w^2 - 2z$ if $w = -1$, $z = 5$

$$\begin{aligned}w^2 - 2z &= (-1)^2 - 2 \times 5 \\ &= 1 - 10 \\ &= -9\end{aligned}$$

4. Use the formula $C = \frac{5(F-32)}{9}$ to convert a temperature of 100° in the Fahrenheitsystem to Centigrade.

$$\begin{aligned}C &= \frac{5(F-32)}{9} \\ &= \frac{5(100-32)}{9} \\ &= \frac{5(68)}{9} \\ &= 37.78\end{aligned}$$

Exercises

1. Evaluate the following

a) $-4k$ if $k = 7$

c) $e^2 - 5$ if $e = 2$

e) $2k^2 + 4$ if $k = -6$

g) $\frac{n}{4} + 2$ if $n = 10$

b) $2mn$ if $m = 4, n = -2$

d) $5 - b + b^2$ if $b = 3$

f) $-3ab^2$ if $a = 4, b = 2$

h) $\frac{u}{5v}$ if $u = -20, v = 2$

2. Evaluate the following if $a = -1, b = 6, c = 3, m = -2, n = 2$

a) $3a^2 - 7$

c) $(2m + 1)^2$

e) $\frac{2m}{n}$

b) $3a - b^2$

d) $3(a^2 + 4)$

f) $(m - n)^2$

Answers

1. a) -28 b) -16 c) -1 d) 11 e) 76 f) -48 g) 4.5 h) -2

2. a) -4 b) -39 c) 9 d) 15 e) -2 f) 16